

STD : 12th SCIENCE	TOPIC : 3,5	MARKS : 30
SUBJECT : MATHS 1	DATE :	

Section A

MCQ **(02)**

1. If L and M are the mid-points of sides BC and CD of parallelogram ABCD, then $\overline{AL} + \overline{AM} =$
 (A) $\frac{1}{2}\overline{AC}$ (B) $\frac{3}{2}\overline{AC}$ (C) \overline{AC} (D) $\frac{2}{3}\overline{AC} \cdot \overline{BD}$
2. In ΔABC , if $a=2$, $\angle B=60^\circ$ and $\angle C=75^\circ$ then $b=$
 (A) $\sqrt{3}$ (B) $\sqrt{6}$ (C) $\sqrt{9}$ (d) $1+\sqrt{2}$

Section B

Solve the following. **(08)**

3. Find the principal solutions of $\cot x = \sqrt{3}$
4. In ΔABC prove that $a(b \cos C - c \cos B) = b^2 - c^2$
5. If the vectors $-3\hat{i} + 4\hat{j} - 2\hat{k}$, $\hat{i} + 2\hat{k}$, $\hat{i} - p\hat{j}$ are coplanar, then find value of p .
6. If $\vec{a}, \vec{b}, \vec{c}$ are the position vectors of the points A, B, C respectively and $5\vec{a} - 3\vec{b} - 2\vec{c} = \vec{0}$, then find the ratio in which C divides the line segment BA.

OR

Find the volume of tetrahedron whose coterminous edges are $7\hat{i} + \hat{k}$, $2\hat{i} + 5\hat{j} - 3\hat{k}$ and $4\hat{i} + 3\hat{j} + \hat{k}$.

Section C

Solve the following. **(12)**

7. Find the general solution of $\sec^2 2x = 1 - \tan 2x$
8. With usual notations prove that $2 \left\{ a \cdot \sin^2 \frac{C}{2} + c \cdot \sin^2 \frac{A}{2} \right\} = a + c - b$

OR

In ΔABC , if $\sin^2 A + \sin^2 B = \sin^2 C$, then show that the triangle is a right angled triangle.

9. If $\vec{a} = \hat{i} + 5\hat{k}$, $\vec{b} = 2\hat{i} + 3\hat{k}$, $\vec{c} = 4\hat{i} - \hat{j} + 2\hat{k}$ and $\vec{d} = \hat{i} - \hat{j}$, find $(\vec{c} - \vec{a}) \cdot (\vec{b} \times \vec{d})$.
10. Express $-\hat{i} - 3\hat{j} + 4\hat{k}$ as a linear combination of the vectors $2\hat{i} + \hat{j} - 4\hat{k}$, $2\hat{i} - \hat{j} + 3\hat{k}$ and $3\hat{i} + \hat{j} - 2\hat{k}$.

Section D

Solve the following. **(08)**

11. In any ΔABC prove that $b^2 = a^2 + c^2 - 2ac \cos B$

OR

11. $\cos^{-1} \frac{12}{13} + \sin^{-1} \frac{3}{5} = \sin^{-1} \frac{56}{65}$
12. If A, B, C, D are four non-collinear points in a plane such that $\overline{AD} + \overline{BD} + \overline{CD} = \vec{0}$, then prove that point D is the centroid of the ΔABC .

OR

12. By vector method prove that the medians of a triangle are concurrent.